

DBLM: Spatiotemporal Resource Management via Deep Black-Litterman Model

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Background

Time Series Supplier Allocation

Time Series Supplier Allocation (TSSA) is to reduce discrepancies and boost efficiency by optimizing supplier capabilities to precisely match order quantities in the future

Black-litterman Model

The Black-Litterman (BL) Model, which originated from the field of financial portfolio management, has a core concept: it incorporates investor subjective perspectives (perspective matrix) to adjust investment decisions, thereby balancing expected returns with investment risks to determine optimal asset allocation ratios.



• DeepLearning

Deep learning (DL) frameworks have emerged as leading solutions to capture non-linear correlations for analysis

Challenges

C1. Spatio-Temporal Dynamics.

As shown in the **GREEN** rectangle, an increase for A whereas a decrease for B compared to their previous levels at time t_{i-1} respectively.

C2. Lack of Supervisory Signals.

Training deep learning models with perspective matrices is challenging due to insufficient supervisory signals, so our focus is developing appropriate training signals.

30 stored, 30 or Future History (30/50)×30 supplied ? t_{i-1} t_{i+1} A's risk value: $t_{i-1} \rightarrow t_i$ Order 50 Order 30 B's risk value: $t_{i-1} \rightarrow t$ C's risk value: $t_{i-1} \rightarrow$ Supply 30 A Supply 20 Order 60 Order 50 E En Supply 50 B B Supply 50 **E** Order 20 ****** There is no order left How should I choose suppliers and allocate Supply 10 my order this time? OK

C3. Data Unreliability.

As shown in the **RED** rectanglethe, the absence of historical orders for **supplier C** obscures their supply potential and associated risks.

The method of DBLM contain four parts:

Data Preparation, STGNN Encoder, Black-Litterman Model and Masked Ranking Loss





Data preparation and STGNN Encoder

Encode the prepared supplier sequence features $\{F_{t-p}, \dots, F_t\}$ and **dynamic propagation matrices** $A_{t-p:t}$ to obtain representations in both spatial and temporal dimensions. Spatial Convolution Layer.

$$\mathcal{H}_t^{(l)} = \sigma\left(\sum_{c=1}^C \mathbf{T}_c(\hat{\mathcal{A}}_t) \mathcal{H}_t^{(l-1)} \mathbf{W}_{\rm sp}^{(l)}\right)$$

Temporal Convolution Layer

$$\mathcal{E}_t^{(l)} = f\left(\mathbf{W}_{te}^{(l)} * \mathcal{E}_{t-1}^{(l-1)} + \mathbf{b}_{te}^{(l)}\right)$$



Black-Litterman Model

• Automatically generate perspective matrices that reflect market dynamics

$$\mathcal{P}_{t} = \tanh\left(\sum_{\hat{\mathcal{A}}_{t}(i,j)>0} \alpha_{ij,t} \hat{\mathcal{A}}_{t}(i,j) [\mathcal{H}_{it}^{(l)} \times \mathcal{E}_{jt}^{(l)}]\right) \qquad \Omega_{t} = \operatorname{diag}\left(\sigma(\mathbf{W}_{\mathrm{om}} \mathcal{P}_{t} \Sigma_{t} \mathcal{P}_{t}^{T} + \mathbf{b}_{\mathrm{om}})\right)$$

• Adjust return and risk parameters based on perspective matrices



Masked Ranking Loss

- Construct ranking loss based on Spearman correlation coefficient
- Introduce masking mechanism to reduce the impact of unreliable data
- Guide model learning through monotonicity optimization

$$\min_{\Theta} \mathcal{L} = \sum_{t=0}^{T_{train}} \sum_{j=t}^{t+f} \frac{6\sum_{i=1}^{N-|\mathcal{S}_j|} (r_{i,\text{risk}}^j - r_{i,\text{allo}}^j)^2}{(N-|\mathcal{S}_j|) ((N-|\mathcal{S}_j|)^2 - 1)} + \eta ||\Theta||^2$$

Experiment

Dataset

The MCM dataset comprises supply and order data from 401

suppliers over 240 weeks,

The SZ dataset includes data from 218 suppliers across 2 years (731 days).

DBLM shows outstanding performance and achieves state-of-the-art scores on almost all metrics.

Method	Dataset	MCM-TSSA				SZ-TSSA			
	Metric	HR@10	HR@20	HR@50	MRE	HR@10	HR@20	HR@50	MRE
Baselines	HA	0.045 ± 0.087	0.125 ± 0.058	0.268 ± 0.049	0.968 ± 0.092	0.039 ± 0.086	0.104 ± 0.117	0.230 ± 0.099	0.929 ± 0.087
	MC	0.053 ± 0.096	0.148 ± 0.072	0.276 ± 0.087	0.924 ± 0.053	0.059 ± 0.147	0.141 ± 0.152	0.245 ± 0.104	0.859 ± 0.057
	Greedy	0.078 ± 0.050	0.166 ± 0.061	$\overline{0.307} \pm 0.044$	$\overline{0.902} \pm 0.108$	0.072 ± 0.088	0.154 ± 0.120	0.349 ± 0.109	0.995 ± 0.149
	DP	0.075 ± 0.082	0.155 ± 0.070	0.303 ± 0.053	$0.930 {\pm} 0.124$	0.069 ± 0.075	$0.137 {\pm} 0.096$	$0.346 {\pm} 0.142$	0.942 ± 0.155
	Fuzzy-AHP	0.204 ± 0.197	0.241 ± 0.132	0.311 ± 0.155	0.897 ± 0.162	0.169 ± 0.098	0.217 ± 0.133	0.306 ± 0.129	0.742 ± 0.140
	Fuzzy-TOPSIS	0.104 ± 0.128	0.187 ± 0.140	0.233 ± 0.165	0.887 ± 0.143	0.095 ± 0.087	0.127 ± 0.094	0.149 ± 0.138	0.939 ± 0.143
	Markowitz	0.139 ± 0.170	0.227 ± 0.158	0.309 ± 0.106	0.997 ± 0.191	0.118 ± 0.149	0.154 ± 0.110	0.289 ± 0.128	0.844 ± 0.185
	$ \overline{DT}$ $ -$	0.040 ± 0.492	0.098 ± 0.524	$\overline{0.204 \pm 0.460}$	0.974 ± 0.680	0.038 ± 0.612	0.106 ± 0.598	0.206 ± 0.720	0.977 ± 0.749
	Lasso	0.066 ± 0.544	0.137 ± 0.670	0.296 ± 0.399	0.872 ± 0.721	0.061 ± 0.482	0.161 ± 0.670	$0.350 {\pm} 0.648$	$0.736 {\pm} 0.725$
	MLP	0.199 ± 0.344	0.245 ± 0.287	0.331 ± 0.225	0.973 ± 0.339	0.182 ± 0.291	$0.246 {\pm} 0.348$	$0.382 {\pm} 0.306$	0.556 ± 0.320
	ECM	0.272 ± 0.282	0.289 ± 0.299	0.348 ± 0.310	0.641 ± 0.407	0.253 ± 0.238	$0.290 {\pm} 0.288$	$0.412 {\pm} 0.271$	0.493 ± 0.377
	SGOMSM	0.263 ± 0.397	0.311 ± 0.403	0.327 ± 0.454	$0.844 {\pm} 0.429$	0.204 ± 0.140	$0.282 {\pm} 0.198$	$0.369 {\pm} 0.245$	0.671 ± 0.298
	AGA	0.158 ± 0.237	0.206 ± 0.228	0.310 ± 0.296	0.772 ± 0.357	0.180 ± 0.205	0.242 ± 0.167	0.374 ± 0.152	$0.629 {\pm} 0.261$
Ours	DBLM	0.403 ±0.284	$\textbf{0.449}{\pm}0.293$	0.487 ± 0.356	$\textbf{0.518}{\pm}0.292$	0.481 ± 0.158	$0.543{\pm}0.187$	$0.662{\pm}0.182$	0.327 ±0.323
Ablation	DBLM(w/o BL)	0.154 ± 0.488	0.238 ± 0.462	0.347 ± 0.529	0.820 ± 0.442	0.112 ± 0.658	0.148 ± 0.495	0.325 ± 0.431	$0.729 {\pm} 0.480$
	DBLM (w/o STGNN)	0.306 ± 0.280	0.348 ± 0.305	0.377 ± 0.340	0.852 ± 0.319	0.274 ± 0.144	0.309 ± 0.195	0.420 ± 0.170	$0.438 {\pm} 0.266$
	DBLM (w/o TCN)	0.314 ± 0.277	0.370 ± 0.284	0.393 ± 0.342	0.648 ± 0.320	0.293 ± 0.109	0.341 ± 0.132	0.448 ± 0.240	0.361 ± 0.258
	DBLM (w/o DGCN)	0.323 ± 0.211	0.419 ± 0.277	0.431 ± 0.330	0.719 ± 0.376	0.340 ± 0.172	0.442 ± 0.249	0.473 ± 0.150	0.377 ± 0.342
	DBLM (w/o Fusion)	0.379 ± 0.299	0.420 ± 0.311	0.453 ± 0.328	$0.588 {\pm} 0.347$	0.364 ± 0.455	0.425 ± 0.298	$0.588 {\pm} 0.211$	0.367 ± 0.243
	DBLM (w/o Mask)	0.376 ± 0.280	0.390 ± 0.246	0.426 ± 0.359	$0.626 {\pm} 0.341$	0.349 ± 0.240	$0.426 {\pm} 0.328$	0.539 ± 0.331	$0.427 {\pm} 0.397$
	DBLM (w/o Rank Loss)	0.290 ± 0.279	$0.317 {\pm} 0.194$	0.335 ± 0.243	0.692 ± 0.287	0.307 ± 0.198	$0.373 {\pm} 0.276$	$0.501 {\pm} 0.453$	$0.486 {\pm} 0.493$

Summary

- DBLM is the first initiative to integrate financial investment management strategies with supply chain demand challenges.
- We introduce a novel masked ranking loss to guide the training of DBLM, which is implemented by the Spearman rank correlation coefficient.
- Our comprehensive experimental evaluation on two supplier allocation datasets demonstrates the superior performance of DBLM over existing baselines.



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Thank You !!!

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